

# RanCompute: Computational Security in Embedded Devices via Random Input and Output Encodings



**Georgia Tech** School of Electrical and  
Computer Engineering

KEVIN HUTTO<sup>^</sup>, SANTIAGO GRIJALVA\*, AND VINCENT JOHN MOONEY III &  
<sup>&</sup>ASSOCIATE \*PROFESSOR, <sup>^</sup>SCHOOL OF ELECTRICAL AND COMPUTER ENGINEERING  
<sup>&</sup>ADJUNCT ASSOCIATE PROFESSOR, SCHOOL OF COMPUTER SCIENCE  
<sup>^</sup>,\*,&INSTITUTE FOR INFORMATION SECURITY AND PRIVACY  
GEORGIA TECH, ATLANTA, GA 30332-0250

*presented at MECO'2022 and CPSIoT'2022, Budva, Montenegro*

[www.mecoconference.me](http://www.mecoconference.me)



# Outline

2

- **Problem Definition**
- **Approach**
- **Example Computations**
- **Results**
- **Conclusions**
- **References**

# Outline

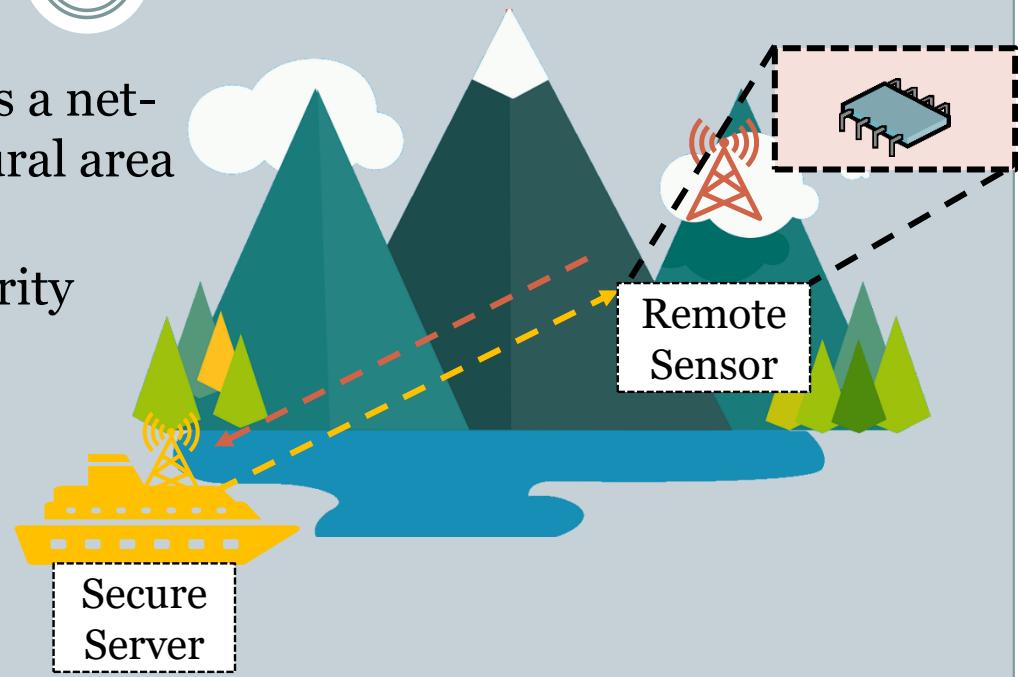
3

- Problem Definition
- Approach
- Example Computations
- Results
- Conclusions
- References

# Problem Definition

4

- Consider a remote network, such as a network of sensors dispersed over a rural area
- The sensor is one of many in an environment with no physical security
- A capable adversary may capture one or more of the remote sensor(s) and attempt to reverse engineer the logic (including reconfigurable logic) and memory contents through state-of-the-art techniques [1][2]
- We consider a microchip architecture implementing one of two possible applications
- We aim to hide which of the two possible applications is being performed on the microchip given an adversary with complete white-box access at a specific time of capture



# Outline

5

- Problem Definition
- Approach
- Example Computations
- Results
- Conclusions
- References

# Approach

6

- One aspect which helps to hide the identity of a digital computation is to have truth tables with identical output frequencies
  - Output frequency – the number of times (multiplicity) a specific output appears in all possible outputs (including repeat values) resulting from a function  $F_m()$  given a finite input set [3]
- We add a minimum number of encodings to ensure matching output frequencies of two target computations

A	B	$F_1(A, B) = A + B$
0	0	0 ( $S_0^1$ )
0	1	1 ( $S_1^1$ )
1	0	1 ( $S_1^1$ )
1	1	2 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	0 ( $S_0^2$ )
0	1	0 ( $S_0^2$ )
1	0	0 ( $S_0^2$ )
1	1	1 ( $S_1^2$ )



A	B	$F_1(A, B) = A + B$
0	0	00 ( $S_0^1$ )
0	1	01 ( $S_1^1$ )
1	0	01 ( $S_1^1$ )
1	1	10 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	00 ( $S_{0a}^2$ )
0	1	01 ( $S_{0b}^2$ )
1	0	01 ( $S_{0b}^2$ )
1	1	10 ( $S_1^2$ )

# Approach (continued)

7

A	B	$F_1(A, B) = A + B$
0	0	0 ( $S_0^1$ )
0	1	1 ( $S_1^1$ )
1	0	1 ( $S_1^1$ )
1	1	2 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	0 ( $S_0^2$ )
0	1	0 ( $S_0^2$ )
1	0	0 ( $S_0^2$ )
1	1	1 ( $S_1^2$ )

$S_0^1$  = Symbol representing zero for function  $F_1$

$S_{0a}^2$  = Symbol representing zero for function  $F_2$ , version *a*

$S_{0b}^2$  = Symbol representing zero for function  $F_2$ , version *b*

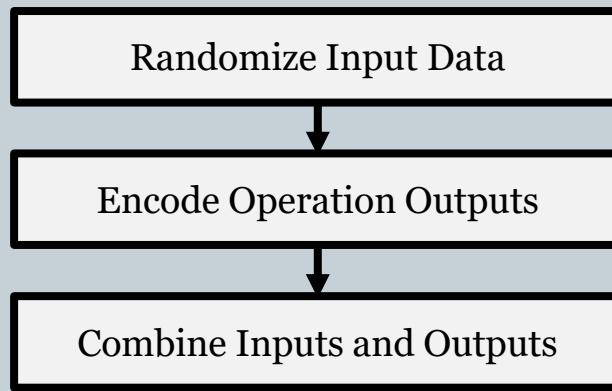


A	B	$F_1(A, B) = A + B$
0	0	00 ( $S_0^1$ )
0	1	01 ( $S_1^1$ )
1	0	01 ( $S_1^1$ )
1	1	10 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	00 ( $S_{0a}^2$ )
0	1	01 ( $S_{0b}^2$ )
1	0	01 ( $S_{0b}^2$ )
1	1	10 ( $S_1^2$ )

# Approach (continued 2)

8



A	B	$F_1(A, B) = A + B$
0	0	00 ( $S_0^1$ )
0	1	01 ( $S_1^1$ )
1	0	01 ( $S_1^1$ )
1	1	10 ( $S_2^1$ )

A	B	$F_1(A, B) = A + B$
0	0	$S_0^1$
0	1	$S_1^1$
1	0	$S_1^1$
1	1	$S_2^1$

A	B	$F_1(A, B) = A + B$
0	0	10 ( $S_0^1$ )
0	1	11 ( $S_1^1$ )
1	0	11 ( $S_1^1$ )
1	1	00 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	0 ( $S_0^2$ )
0	1	0 ( $S_0^2$ )
1	0	0 ( $S_0^2$ )
1	1	1 ( $S_1^2$ )

A	B	$F_2(A, B) = A * B$
0	0	$S_{0a}^2$
0	1	$S_{0b}^2$
1	0	$S_{0b}^2$
1	1	$S_1^2$

A	B	$F_2(A, B) = A * B$
0	0	10 ( $S_{0a}^2$ )
0	1	11 ( $S_{0b}^2$ )
1	0	11 ( $S_{0b}^2$ )
1	1	00 ( $S_1^2$ )

(a) Standard Unsigned Binary Operations

(b) Outputs Assigned Symbols to Match Frequencies

(c) Output Symbols Replaced With New Bit-Representations

# Approach (continued 3)

(b) Encode Operation Outputs

9

A	B	$F_1(A, B) = A + B$
0	0	00 ( $S_0^1$ )
0	1	01 ( $S_1^1$ )
1	0	01 ( $S_1^1$ )
1	1	10 ( $S_2^1$ )

A	B	$F_1(A, B) = A + B$
0	0	$S_0^1$
0	1	$S_1^1$
1	0	$S_1^1$
1	1	$S_2^1$

A	B	$F_1(A, B) = A + B$
0	0	10 ( $S_0^1$ )
0	1	11 ( $S_1^1$ )
1	0	11 ( $S_1^1$ )
1	1	00 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	0 ( $S_0^2$ )
0	1	0 ( $S_0^2$ )
1	0	0 ( $S_0^2$ )
1	1	1 ( $S_1^2$ )

A	B	$F_2(A, B) = A * B$
0	0	$S_{0a}^2$
0	1	$S_{0b}^2$
1	0	$S_{0b}^2$
1	1	$S_1^2$

A	B	$F_2(A, B) = A * B$
0	0	10 ( $S_{0a}^2$ )
0	1	11 ( $S_{0b}^2$ )
1	0	11 ( $S_{0b}^2$ )
1	1	00 ( $S_1^2$ )

(a) Standard Unsigned Binary Operations

(b) Outputs Assigned Symbols to Match Frequencies

(c) Output Symbols Replaced With New Bit-Representations

# Approach (continued 4)

10

(a) Randomize Input Data

A	B	$F_1(A, B) = A + B$
0	0	0 ( $S_0^1$ )
0	1	1 ( $S_1^1$ )
1	0	1 ( $S_1^1$ )
1	1	2 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	0 ( $S_0^2$ )
0	1	0 ( $S_0^2$ )
1	0	0 ( $S_0^2$ )
1	1	1 ( $S_1^2$ )

A	B	$F_1(A, B) = A + B$
1	0	00 ( $S_0^1$ )
1	1	01 ( $S_1^1$ )
0	0	01 ( $S_1^1$ )
0	1	10 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
1	0	00 ( $S_{0a}^2$ )
1	1	01 ( $S_{0b}^2$ )
0	0	01 ( $S_{0b}^2$ )
0	1	10 ( $S_1^2$ )

(b) Encode Operation Outputs

A	B	$F_1(A, B) = A + B$
0	0	0 ( $S_0^1$ )
0	1	1 ( $S_1^1$ )
1	0	1 ( $S_1^1$ )
1	1	2 ( $S_2^1$ )

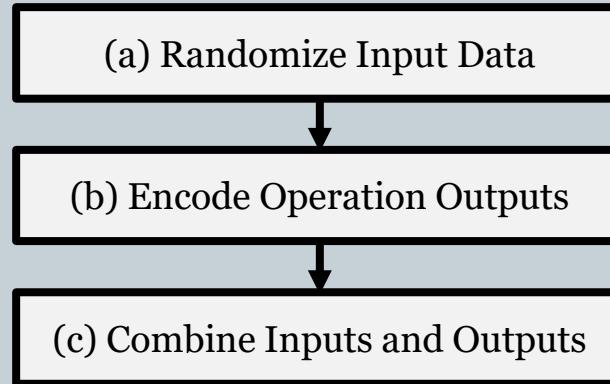
A	B	$F_2(A, B) = A * B$
0	0	0 ( $S_0^2$ )
0	1	0 ( $S_0^2$ )
1	0	0 ( $S_0^2$ )
1	1	1 ( $S_1^2$ )

A	B	$F_1(A, B) = A + B$
0	0	10 ( $S_0^1$ )
0	1	11 ( $S_1^1$ )
1	0	11 ( $S_1^1$ )
1	1	00 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	10 ( $S_{0a}^2$ )
0	1	11 ( $S_{0b}^2$ )
1	0	11 ( $S_{0b}^2$ )
1	1	00 ( $S_1^2$ )

# Approach (continued 5)

11



A	B	$F_1(A, B) = A + B$
0	0	0 ( $S_0^1$ )
0	1	1 ( $S_1^1$ )
1	0	1 ( $S_1^1$ )
1	1	2 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
0	0	0 ( $S_0^2$ )
0	1	0 ( $S_0^2$ )
1	0	0 ( $S_0^2$ )
1	1	1 ( $S_1^2$ )



A	B	$F_1(A, B) = A + B$
1	0	10 ( $S_0^1$ )
1	1	11 ( $S_1^1$ )
0	0	11 ( $S_1^1$ )
0	1	00 ( $S_2^1$ )

A	B	$F_2(A, B) = A * B$
1	0	10 ( $S_{0a}^2$ )
1	1	11 ( $S_{0b}^2$ )
0	0	11 ( $S_{0b}^2$ )
0	1	00 ( $S_1^2$ )

# Approach (continued 5)

12

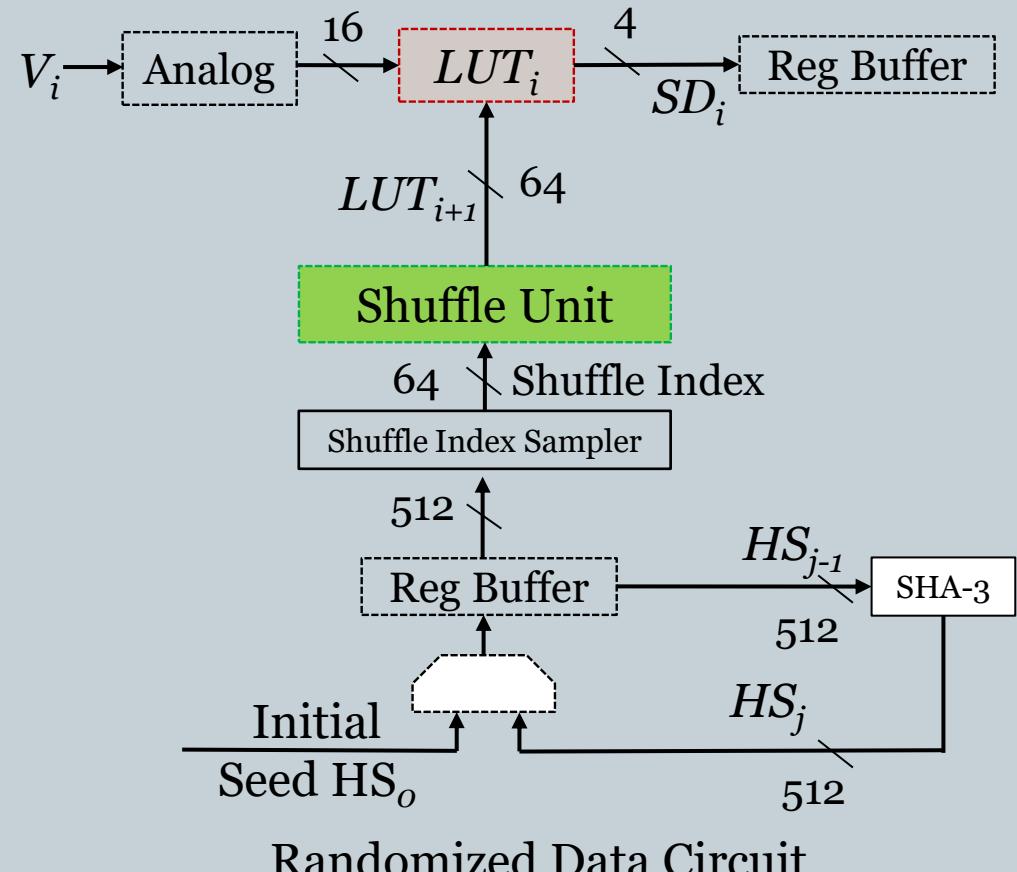
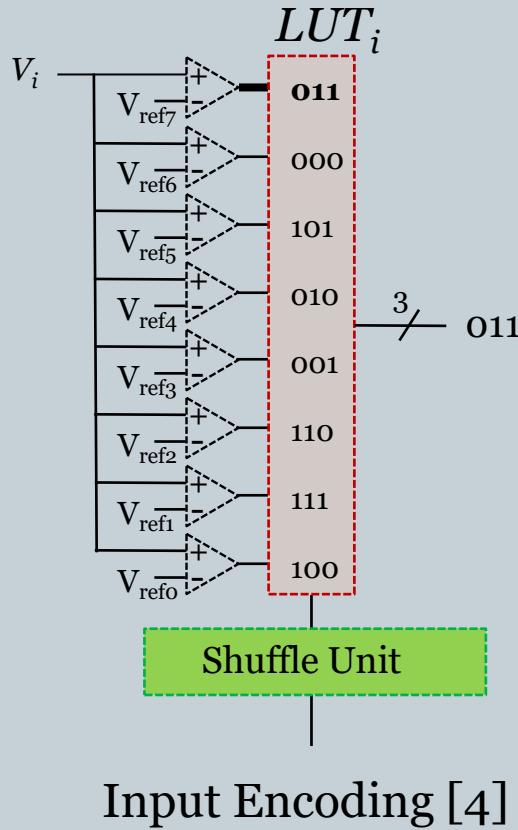
- Look-Up Table (LUT) result for each of the operations with randomized inputs and randomized outputs equalized for frequency

<b>A</b>	<b>B</b>	$F_1(A, B)$ $= A + B$
0	0	11 ( $S_1^1$ )
0	1	00 ( $S_2^1$ )
1	0	10 ( $S_0^1$ )
1	1	11 ( $S_1^1$ )

<b>A</b>	<b>B</b>	$F_2(A, B)$ $= A * B$
0	0	11 ( $S_{0b}^2$ )
0	1	00 ( $S_1^2$ )
1	0	10 ( $S_{0a}^2$ )
1	1	11 ( $S_{0b}^2$ )

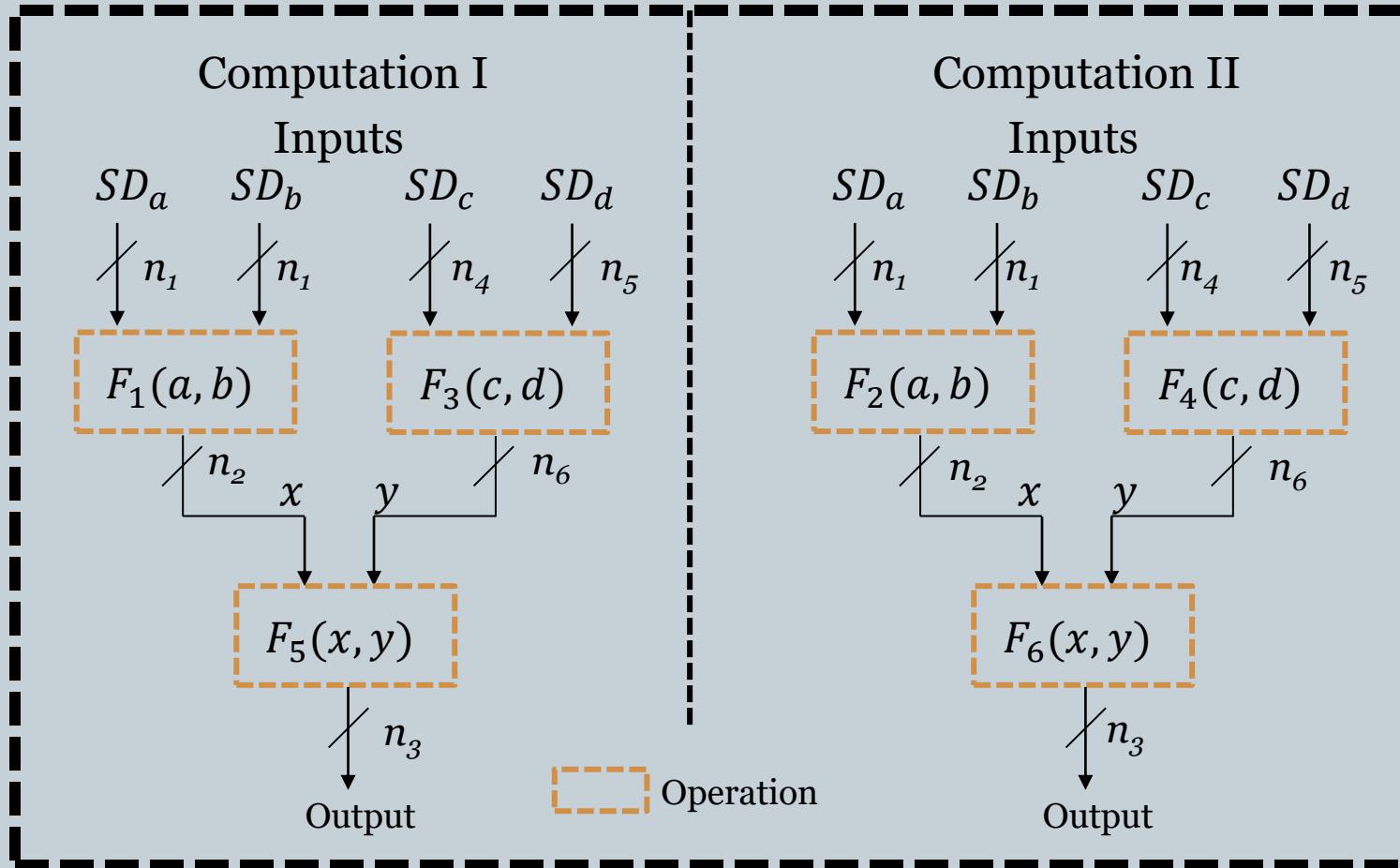
# Method of Input Encoding

13



# Performing Computations

14



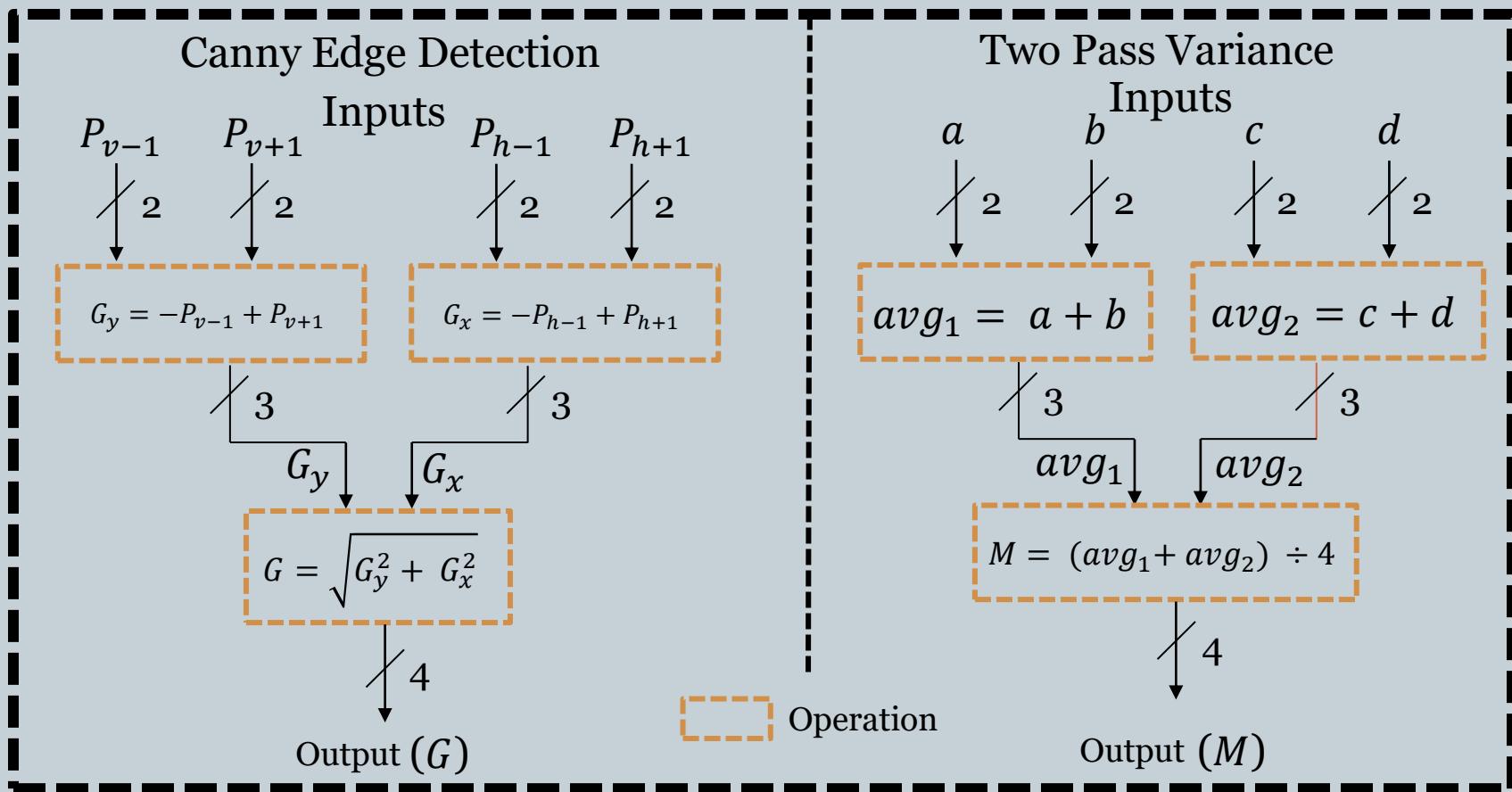
# Outline

15

- Problem definition
- Approach
- Example Computations
- Results
- Conclusions
- References

# Example Computations

16



# Example Computations

17

**Canny Edge Detection  
(Two 3-bit Input Operation)**

(a) Unencoded Output ( $G$ )	(b) $f_i^1$	(c) $f_i^1 \cup f_{ij}^1$
0	4	2, 2
1	8	8
1.5	4	4
2	16	1, 2, 6, 7
3	20	1, 3, 3, 6, 7
3.5	8	8
4	4	4

**Two-Pass Variance  
(Two 3-bit Input Operation)**

(a) Unencoded Output ( $M$ )	(b) $f_i^2$	(c) $f_i^2 \cup f_{ij}^2$
0	1	1
0.25	2	2
0.5	3	3
0.75	6	6
1	7	7
1.25	8	8
1.5	10	2, 4, 4
1.75	8	8
2	7	7
2.25	6	6
2.5	3	3
2.75	2	2
3	1	1

- Output frequencies for the operations with two 3-bit Inputs for Canny Edge Detection and Two-Pass Variance
- Resulting output frequencies:  
(1,1,2,2,2,3,3,4,4,6,6,7,7,8,8)
- Note that the total number of outputs is 64

# Outline

18

- Problem definition
- Approach
- Example Computations
- Results
- Conclusions
- References

# Results

19

- For each developed RanCompute application, we tested 10,000 iterations
- All simulations showed expected functionality, with the output of each RanCompute application equaling the expected encoding

FGPA UTILIZATION OF RANCOMPUTE				
Application	Slice LUTs	Slice Regs	Bonded IOB	Max Freq.
(a)	2	3	10	450 MHz
(b)	6	5	14	450 MHz
(c)	5	1	18	380 MHz
(d)	8	4	15	450 MHz
(e)	13	1	22	380 MHz
(f)	120	7	26	380 MHz

- (a) Two 2-bit input logic functions (add, multiply)
- (b) Two 3-bit input logic functions (add, multiply)
- (c) Two 4-bit input logic functions (add, multiply)
- (d) 2-bit Edge Detection / Variance
- (e) 3-bit Edge Detection / Variance
- (f) 4-bit Edge Detection / Variance

# Outline

20

- Problem definition
- Approach
- Example Computations
- Results
- Conclusions
- References

# Conclusions

21

- In this paper we introduced a novel methodology to perform computations which are indistinguishable from each other from the point of view of an adversary with reverse engineering capabilities.
- We believe this is an important first step in the development of a framework for a general purpose method to perform indistinguishable computations on a microchip.

# Outline

22

- Problem definition
- Approach
- Example Computations
- Results
- Conclusions
- References

# References

23

- [1] “Technical Capabilities,” 2021. [Online.] Available: <https://www.techinsights.com/technical-capabilities>
- [2] A. Duncan et al., “FPGA Bitstream Security: A Day in the Life,” *2019 IEEE International Test Conference* (ITC ’19), 2019, pp. 1-10.
- [3] W. D. Blizzard et al., “Multiset Theory,” *Notre Dame Journal of Formal Logic*, Vol. 30, No. 1, pp. 36-66, 1989.
- [4] K. Hutto and V. Mooney, “Sensing with Random Encoding for Enhanced Security in Embedded Systems,” *2021 10<sup>th</sup> Mediterranean Conference on Embedded Computing* (MECO ’21), Vol. 10, pp. 809-814, 7 June 2021.
- [5]-[16] *Please see the paper for these references.*

# THANK YOU

24

## Q&A

**Kevin Hutto**  
[khutto30@gatech.edu](mailto:khutto30@gatech.edu)

**Santiago Grijalva**  
[sgrijalva@ece.gatech.edu](mailto:sgrijalva@ece.gatech.edu)

**Vincent Mooney**  
[mooney@ece.gatech.edu](mailto:mooney@ece.gatech.edu)